Universitat Politècnica de Cataluña (UPC) Department of Signal Theory and Communications

LIDAR Sensing of the Atmosphere:

RECEIVER DESIGN AND INVERSION ALGORITHMS FOR AN ELASTIC SYSTEM.

Doctor-Engineer Thesis

Francesc Rocadenbosch Burillo

Director: Dr. Adolfo Comerón Tejero

November 1996

Barcelona, (SPAIN)

Dr. JAVIER BARA TELLES (PRESIDENTE) Dr. JUAN JOSÉ JIMÉNEZ LIDON (VOCAL)

Dr. JOSE MARÍA BALDASANO RECIO (VOCAL) JABORDANO

Dr. MANUEL BETANGER GARCÍA (VOCAL)

W. PREJORI VAZILLE TRAU (SECRETARIO)

[Mitrasaton :

Apto "cum lande" (for unamendad) Baralona, 16 de draembe de 1996

UNIVERSITAT SOLITECTUCA DE CATALUNYA AD MINI T. A. I.) D'A CUMERICS ACADÈMICS

Acurista Tesi la estet enrecistrada a la pàgina 16 amb el número 849

Barcelona, 15 - 1 - 97

L'ENCARRECAT DAL PEGISTRE,



Universitat Politècnica de Cataluña (UPC) Department of Signal Theory and Communications

LIDAR Sensing of the Atmosphere:

RECEIVER DESIGN AND INVERSION ALGORITHMS FOR AN ELASTIC SYSTEM.

Doctor-Engineer Thesis

Francesc Rocadenbosch Burillo

BIBLIOTECA RECTOR GABRIEL FERRATÉ

Director: Dr. Adolfo Comerón Tejero

November 1996

Barcelona, (SPAIN)

To my parents, Encarna and grandparents Isidre and María. This work has been supported by the Spanish Interministry Committee for Science and Technology, CICYT, grant number TIC 431-93.

Thanks are due to the
Institute of Technology and Environmental Modelling (ITEMA)
and the following Administrations:
Diputació de Barcelona, City Council and Entitat del Medi Ambient.

Preface

History is not made by kings and presidents but by ordinary people doing extraordinary things.

TIMES magazine, Aug. 1996

I am indebted to many people who have contributed material, ideas and offered encouragement during this PhD thesis. I would like to offer special thanks to my thesis director and colleague, professor Adolfo Comerón for his confidence during these three years of work, support and willingness to experiment; to professor Gregori Vázquez for his technical help with the Kalman filter and to professor José María Baldasano, head of the Institut de TEcnologia i Modelització Ambiental (ITEMA). I am also particularly grateful to the Escola Universitaria Politècnica del Baix Llobregat and his director, professor Javier Bará, for the large number of resources and means facilitated, both technical in its well equipped laboratories and administrative; to professor Ferrán Canal, who has been sharing the laboratory of Integrated Optics with the LIDAR activity; to professor Don Fay at Queen's University of Belfast for his generous help in proof-reading the draft-copy of this thesis and patient correction of english mistakes and to professor Ramón Pallás for the selected material made available about CF amplifiers and the instrumentation borrowed from the Electronics Department. I also appreciate the company, friendship and helpful collaboration of Carles Puente and Alejandro Rodríguez, members of the lidar team, with whom I have shared many adventures and who have mainly worked in optical and Doppler lidar activities, respectively, and the kind cooperation of Cecilia Soriano at ITEMA. I also appreciate the help and commitment of all the Department staff, in particular, I do thank Joaquim Giner and Alfredo Cano, for their neat work with the lidar receiver, electrical installation and mechanization of some parts of the lidar system; our computer system manager, Josep Maria Haro, for the installation and preparation of the lidar control computer and Juanjo Tomeo for the promptly and ready work in the activities developed. I wish to acknowledge especially the inputs from the following project students under my direction: Alejandro Lansac Catalán, Matthias Thyroff, Joan Manuel Medina Mesa, Joan Capdevila Vives, Raquel Barrera Moreno, Iván Campos Avilés who worked in the area of system development an integration, Joan Manel March i Gonzàlez and Enric Martín Bayes in the area of atmospheric propagation, Daniel Pineda Masnou, Josep Roca Gabarrón, Alex Sanchez Palaso in the area of inversion and imaging algorithms and also the collaboration of Carles Céspedes and Enric Jornet.

Special thanks are due to the CICYT, which has financially backed the work under the grant TIC 431-93.

Finally, I wish to offer special thanks to my parents and Encarna for they patience, help and understanding in very many ways and to my friend and colleague Adriano Camps for his appreciation and helpful art comments.



UNIVERSITAT POLITÈCNICA DE CATALUNYA

Department of Signal Theory and Communications Address: c/. Gran Capità, s/n
Campus Nord UPC - Edifici D-3
08034 Barcelona - Spain
Telephone: 34-3-401 68 49
Telefax: 34-3-401 72 32

Abstract

LIDAR is an acronym of **LI**ght Detection And Ranging. In the present case, the elastic lidar techniques are used to remotely sense the atmosphere and to derive quantitative information about its optical parameters.

This thesis comprises the design and operation of an elastic lidar station based on a pulsed *Nd:YAG* laser operating at the *1064-* and *532-nm* wavelengths, in the parts concerning receiver, control systems and inversion algorithms.

Basically, it can be divided in three different parts. The first one (Chaps.1,2,3) encompass the study of the elastic scattering (Rayleigh and Mie) in the atmosphere for link-budget purposes and gives some insight into the interweaving between physical variables such as temperature, pressure and humidity and the scattering phenomena, letting apart any possible extrapolation to meteorological models. From this basis, extinction and backscatter figures for different atmospheric conditions can readily be assessed and as a result a system linked budget is presented. This includes lidar range study, signal-to-noise ratio assessment and photodiode evaluation from custom-made libraries. At the end of the first part system specification is made.

The second part of this work (Chaps.4,5,6) is concerned with the design and implementation of the receiver, synchronization and control systems. The optoelectronic receiver is based on current-feedback amplifiers and features very large gain-bandwidth product. As for the synchronization subsystem, two different units are presented with a view to a future lidar mobile systems, which make room for interspersed scans. Finally, the control system designed is LabView-based and features a distributed control philosophy. For that purpose, lidar bus protocols and signal are specified and built for the actual lidar station.

Finally, the third part encircles the design of inversion algorithms with and without memory (Chaps.7,8). Nonmemory algorithms for homogeneous atmospheres are based on regression curve fitting procedures, such as slope-method and least squares and in instances of inhomogeneous atmospheres they are based on Klett's method and appropriate calibrations. Memory algorithms are based on different stochastic models for the atmosphere and on nonlinear Kalman filtering. In addition to the inversion procedures, error assessment plots are also derived and discussed. Chap.9 describes the measurements carried out with the system this work has contributed to build and the results of applying to them the inversion algorithms discussed in the preceeding chapters.

The inversion of live-scenes involves pollution structure studies, cloud studies (ceilometry, cloud motion and wave clouds, basically) and hints overlap factor error sources.

Francesc Rocadenbosch-Burillo

Contents

INTRODUCTION	XV
INTRODUCTION	21. 4
1 I ACED CYCTEMS AS DEMOTE SENSODS AND THE LIBS LIBAR	
1. LASER SYSTEMS AS REMOTE SENSORS AND THE UPC LIDAR	1.1
1. Remote sensing using optical radars	
2. Optical requirements for laser radars	
2.1 Atmospheric transmission windows	
2.2 Optical interaction of lasers with atmospheric species 1.3	
2.3 Laser sources	
2.4 Detectors	
3. Remote monitoring capabilities of lidar systems 1.8	
3.1 Single-ended systems	
3.1.1 Elastic-backscatter lidar 1.8	
3.1.2 Differential-absorption lidar (DIAL) 1.9	
3.1.3 Fluorescence lidar 1.11	
3.1.4 Raman scattering lidar 1.12	
3.1.5 Doppler lidar 1.12	
3.2 Double-ended systems	
3.2.1 Bistatic lidar 1.13	
3.2.2 Long-path absorption 1.13	
4. The UPC lidar system	
4.1 Emission configuration 1.14	
4.2 Receiver systems	
4.3 Acquisition and control systems 1.20	
4.4 Synchronization unit 1.22	
2. LIGHT SCATTERING AND RADIANCE IN THE ATMOSPHERE	2.1
1. Madala in a standard stress how as provinced in	
1. Models in a standard atmosphere approximation 2.1	
1.1 Standard atmosphere models	
1.2 Data example for Barcelona 2.6 2. Rayleigh scattering dependency on the	
atmospheric variables 2.8	
2.1 Review of Rayleigh scattering 2.8	
2.2 Rayleigh scattering in a standard atmosphere 2.10	
2.3 Inclusion of pollutant sources	

	3. Mie scattering	
	3.1 Monodispersions	
	3.1.1 Review of Mie scattering 2.14	
	3.1.2 Simulation of monodispersions with	
	link-atmos 2.17	
	3.2 Polydispersions	
	3.2.1 Optical parameters in polydispersions 2.19	
	3.2.2 Distribution functions 2.20	
	4. Hints to build lidar link-budget-oriented	
	atmospheric models 2.22	
	4.1 Barcelona city example 2.22	
	4.2 Inclusion of humidity effects 2.24	
	4.3 Height dependency	
	5. The background radiance	
	5.1 Noisy sources	
	5.2 Celestial coordinates	
	5.3 Solar radiation	
	5.4 Moon's radiation	
B. LI	NK-BUDGET AND SYSTEM SPECIFICATIONS	3.1
	1. Link-budget oriented lidar equations	
	1.1 The basic lidar equation	
	1.2 Simple overlap factor	
	1.3 The visibility margin approach 3.7	
	1.4 Design comments and default values concerning	*
	this section	
	2. Signal-to-noise ratio assessment in the lidar receiver 3.11	
	2.1 Noise statistics for an APD-amplifier module 3.11	
	2.2 Signal-to-noise ratio of the lidar receiver 3.14	
	2.3 Choosing the right detector	
	2.4 Noise limited modes and SNR 3.18	
	2.5 The lidar receiver and signal-to-noise	
	ratio enhancement	
	2.5.1. Philosophy of the lidar receiver 3.19	
	2.5.2. The M-G domain	
	2.5.2. The M-G domain	
	2.6 Default values concerning this section 3.25	
	3. Lidar range estimation	
	3.1 Absolute minimum and maximum exploring	
	ranges of the system 3.27	
	3.2 The exploring window	
	3.3 Gain and synchronism specs	
	4. A glance to link-budget software	

4. THE LIDAR RECEIVER	4.1
1. Specifications overview 4.1 2. Sensing circuits for the lidar front-end 4.1 2.1 I-V characteristics 4.1 2.2 Practical transimpedance amplifiers 4.4 3. Transimpedance stage 4.7 4. Conditioning stage 4.10 5. Offset compensation stage 4.14 5.1 Operation modes 4.14 5.2 Offset level and drift rate assessment in normal mode 4.15 5.3 Reference for the auto-zero unit 4.16 6. Prototype and final measurements 4.19 6.1 Mechanical overview 4.19 6.2 Bandwidth measurement 4.19 6.3 Noise measurements 4.21	
5. TEST & MEASUREMENT OF THE APD	5.1
1. Illumination of the active area 5.1 1.1 Measurement wavelength and correction factors 5.1 1.2 Illumination of the active area 5.2 2. Quantum efficiency measurement 5.4 2.1 Procedure and experimental set-up 5.4 2.2 Results 5.4 2.3 Extended error analysis 5.5 3. Multiplication factor measurement 5.6 3.1 Procedure and experimental set-up 5.6 3.2 Results 5.8 3.3 Extended error analysis 5.10 4. Mean responsivity computation 5.11 5. Local variations within the active area 5.12 5.1 Local variations of the responsivity 5.12 5.1.2 Results 5.13 5.2 Local variations of the multiplication factor 5.14 5.3 Error analysis 5.14 6. Dark current components 5.15 7. Noise spectral densities 5.16 7.1 Procedure and test set-up 5.16	
7.2 Results	

VII		Contento
XII		Contents.

	EM INTEGRATION AND TEST SET-UP: CHRONIZATION AND CONTROL UNITS	6.1
1	. Lidar system integration 6.1	
1.	1.1 System overview 6.1	
	1.2 Laser synchronization signals system 6.5	
	,	
	r	
	1.3.1 The lidar bus 6.7	
0	1.3.2 Other protocol signals 6.7	
2.	The synchronization unit 6.9	
	2.1 Specification overview 6.9	
	2.2 Functional diagram and operation 6.9	
	2.3 Buffered synchronization unit 6.13	
	2.3.1 Timing module 6.13	
	2.3.2 Buffer module 6.18	
	2.3.3 Test and measurement 6.19	
	2.3.4 Calibration model for the sync. unit 6.21	
	2.4 Microprocessor-based synchronization unit 6.22	
3.	. The control unit	
	3.1 The virtual instrument approach 6.25	
	3.2 Acquisition and control cards 6.26	
	3.3 The control program 6.29	
	3.3.1 Raw-data preprocessing 6.29	
	3.3.2 Sync module control 6.30	
4.	System test experiments 6.32	
	4.1 Test set-up	
	4.2 Performance 6.33	
	4.3 Link-budget 6.34	
	4.4 Build-up correction 6.38	
	1.1 band up contection	
7. LIDA	R INVERSION METHODS WITHOUT MEMORY	7.1
1	Lidar inversion grounds 7.1	
	Algorithm ranking points. Some criteria 7.5	
	Slope-method vs. Least-squares	
3.	3.1 Slope-method	
	3.2 The least-squares algorithm 7.10	
	3.3 Evaluation and sensitivity studies 7.11	
	3.3.1 Simulation procedure overview 7.11	
	3.3.2 Noise-sensitivity study 7.12	
	3.4 Hybrid methods: LANL live scene inversion 7.14	
4.	. Klett's method	
	4.1 The algorithm 7.18	

Contents.	XIII
-----------	------

4.2 Evaluation and sensitivity studies 7.20 4.2.1 Calibration error study 7.20 4.2.2 Correlation error study 7.21 4.2.3 Noise-sensitivity study 7.21 4.2.4 Homogeneous atmosphere study 7.23 4.3 LANL live scene inversion 7.23 5. Conclusions 7.24 5.1 About slope-method and least-squares 7.24 5.2 About Klett's method 7.25	
8. LIDAR INVERSION AND NONLINEAR KALMAN FILTERING	8.1
1. Introducing the Kalman filter 8.1 1.1 Linear discrete Kalman filter 8.4 1.2 Extended discrete Kalman filter 8.4 1.3 Relationship to deterministic least-squares 8.7 2. Lidar inversion philosophy using the Kalman filter 8.8 3. First approach to the inversion: 8.9 3.1 The undersampling filter 8.9 3.2 Modelization of the atmosphere 8.10 3.3 The measurement equation 8.11 3.4 Initialization 8.13 3.5 Results 8.14 4. Second approach to the inversion: 8.14 4. Second approach to the inversion: 8.17 4.1 The Gauss-Markov process 8.17 4.2 Modelization of the atmosphere 8.18 4.2.1 Temporal correlation 8.18 4.2.2 Spatial correlation 8.20 4.3 First filter: the constant backscatter estimator 8.24 4.4 Second filter: the markovian estimator 8.28 4.5 Results and discussion 8.30 5. The observability problem 8.37	
9. LIDAR MEASUREMENTS	9.1
1. Overlap factor effects on the measurements	

Contents.

1.4 Inclusion of the Gaussian spot behaviour 9.71.5 Effect of the overlap factor on the measurements 9.8	
1.5.1 Practical considerations 9.8 1.5.2 Backscatter errors 9.10	
2. Practical aspects and limitations of the	
inversion algorithms	
2.1 Inversion by slices	
and Least-Squares algorithms 9.12	
2.1.2 Choosing Klett's parameters 9.13	
2.2 Choosing the right PPI and IP parameters from	
the control unit 9.14	
2.3 Kalman filter practical considerations 9.14	
2.3.1 Physical model uncertainties and	
tracking capacity 9.15	
2.3.2 Parameter observability 9.16	
2.3.3 State-noise covariance matrix assessment . 9.17	
3. Atmospheric structure studies 9.20	
3.1 Day- and night-time observations in visually clear air 9.20	
3.2 Retrieval of extinction and backscatter profiles 9.25	
4. Cloud studies	
4.1 Ceilometry	
4.2 Retrieval of the extinction profile 9.32	
10. CONCLUDING REMARKS AND FUTURE WORK GUIDELINES	10.1
APPENDIX 1: CURRENT-FEEDBACK OP AMPS	AP.1.1
1. The current-feedback operational amplifier AP.1.1	
2. No gain-bandwidth trade-off AP.1.2	
3. Absence of slew-rate limiting AP.1.3	
4. CFA loop gain analysis	
APPENDIX 2: OVERLAP FACTOR TABLES FOR	
UNIFORM ILLUMINATION	AP.2.1
1. Singular points	
2. Asymptotic values	
3. Tables	

REFERENCES

Introduction

Optical probing of the atmosphere through light scattering actually predates the invention of the laser. Nevertheless, the superior qualities in regard to power and collimation of even the early ruby lasers made them obvious replacements for the conventional *searchlights* previously used. It was, however, the development of *Q-switching* by McClung and Hellwarth (1962) that made possible the generation of very short, single pulses of laser energy and thereby range-resolved measurements.

Photons are absorbed and scattered by gas molecules of the atmosphere and also by its particulate or droplet constituents. In the case of energy at the visible or near-infrared wavelengths, such scattering is sufficient to permit application of the radar principle to observations of the atmosphere itself. This principle is referred to as LIDAR, an acronym for LIght Detection And Ranging.

Even in the visibly clear atmosphere backscattered signal from gases and suspended particles at ranges of several kilometres may readily be detected with laser radars or lidars. It is accordingly possible to detect the presence and location of particulate clouds or layers and, by tracking inhomogeneities in particle concentration, to determine atmospheric structure and motion. Today the processes amenable to laser remote sensing include elastic scattering (i.e. incident and backscattered wavelength coincide) such as Rayleigh and Mie, and inelastic scattering (i.e. the backscatter-signal is wavelength shifted) such as Raman. Other techniques based on resonance scattering, fluorescence, absorption, and differential absorption (DIAL) are also used. These techniques will be discussed further in Chap.1.

Remote atmospheric monitoring with lidar provides unique advantages when compared to other methods. Namely, they permit specific applications which would be difficult, if not impossible, using standard instrumentation. Some of these advantages are: non-interference with the source effluent monitoring (no gas sample extraction is required), measurements on a spatial scale comparable with atmospheric model predictions and possibility of measurements at ground level or aloft. Application examples include a lidar system mounted aboard the NASA Shuttle that will make remote measurements of the upper atmosphere, airborne laser fluorosensors that might be used to study the dispersion of water effluents from industrial and municipal treatment plants, or laser bathymetry of coastal regions that could be undertaken from helicopters.

This wide range of applications along with an outgrowing environmental concern grants these systems a relevant role in Europe and particularly in Spain, where they are avant-garde. At the Signal Theory and Communications Dept. of the Polytechnic University of Catalonia (UPC) at Barcelona, Spain, an elastic-backscatter lidar has been developed under the Interministry Committee for Science and Technology (CICYT) grant TIC431-93. The main objective of the project was to gain expertise with the lidar technique, and to develop prototypes in Spain. It is expected this will consolidate a research line encompassing the development of mobile elastic systems, the design of coherent systems allowing the measurement of Doppler shifts, hence the measurement of the radial component of wind velocity, and, in a longer term of lidar systems able to identify chemical species.

XVI Introduction.

Before proceeding further to describe the structure of the chapters, the contents of some of them warrants some comments: This PhD thesis intends to be a report of the author's work in the design of the lidar system, specially in the parts concerning link-budget, receiver systems and inversion algorithms, during the period 1993-1996. In writing this thesis, the author has intended to make it as comprehensive as possible and plenty of references have been included. Yet, since research is an endless activity, some of the circuits presented are being continuously upgraded. In particular, in what regards the inner core of the lidar system electronics, that is, the optoelectronic receiver and the synchronization unit (chapters 4 and 6, repectively), two and sometimes up to three different units of some subsystems have been developed since the beginning of the lidar activities until mid 1996. In the case of the lidar receiver, three different units have been designed and built: two analog and another one digital. Yet, only the latest analog version is reported here because the digital conception is being patented and consequently, it is protected by confidentiality rights.

Next, this is how the different chapters are organized:

The basis of *Chapter 1*, is formed by broad reviews of atmospheric laser remotesensing techniques and applications as well as an introduction to the lidar system developed in the Department. The first part of this chapter has been written with an eye to providing the reader with some insight into the enormous breadth of measurements that can be undertaken remotely with lasers sensors and into the state-of-the-art. The second part is aimed at giving an overview of the goals and architecture of the elastic-backscatter lidar system currently developed.

Remote sensing of the atmosphere from optical parameters (i.e. extinction- and backscatter-coefficient) is deeply linked with meteorological variables (e.g. temperature, pressure, humidity, etc.) and atmospheric ones (e.g. type of aerosols, clouds, rain, etc.). For this reason, the aim of *Chapter 2* is two-fold: First, especial effort has been made to gather as much information as possible about Rayleigh and Mie scattering, and to relate them, in a semi-quantitative manner and under the simplificated conditions of a standard atmosphere, to the physical parameters of temperature, pressure and relative humidity. Nevertheless, it has been possible to pinpoint the interplay between optical and physical parameters. Furthermore, this study has laid the basis of a computation software, which fulfils a double purpose: first, the easy estimation of the optical parameters under different atmospheric conditions such as rain, fog, hazes, clouds, etc. and second, the possibility of making custom-made synthesis of atmospheric profiles that helps error assessment in the lidar inversion algorithms. The second part of this chapter concentrates on the study of the background solar radiation, (that is, scattered solar radiation from either the sky or the ground), that under daytime operation can often dominate all other forms of noise.

Link-budget and system specifications are dealt with in *Chapter 3*. The basic laser remote-sensing equation is considered with particular care about the impact of system optical trade-offs, photodetector selection, receiver parameters and system noise. The problem of signal-to-noise ratio in the system and its optimization is also considered. This has a direct implication for the lidar range assessment. The great quantity of system parameters that have had to be considered have led the development of a second software package, whose applications encompass optical communications links.

In a lidar system, the backscattering radiation gathered by the receiver is transformed into an electrical signal which can be digitally processed to retrieve information about the concentration of aerosols in the air at different distances and heights.

Introduction. XVII

Chapter 4 concentrates on the electrical and mechanical design of the receiver, under the considerations discussed. Beginning with a comprehensive collection of sensing circuits for the lidar front-end, the chapter progresses to the transimpedance configuration in use. Next, the layout and components of the receiver, which basically comprises transimpedance, conditioning and offset correction stages, are discussed step by step. Finally, bandwidth and noise measurements corroborate the design specifications.

Chapter 5 concentrates on the test and measurement of the key device of the receiver system, the photodetector. The measurement span includes not only characteristic parameters such as quantum efficiency, responsivity, gain, dark current and noise, but also local variations of the responsivity and gain over the active area of the device. In addition, test set-ups and error analysis are presented.

Integration of the lidar system into a test set-up architecture is treated in *Chap. 6*. It comprises the following subsystems: laser emitter, receiver unit, synchronization unit and control unit. The purpose of the test set-up is to provide effective range-resolved calibrations and adjust the synchronization among the different units when they are immersed in the lidar system as a whole. Since the mainstay of test procedures involves the synchronization unit and its protocol signals, it has been considered more convenient and adapted to begin with the design of this unit and to continue with the tests conducted. As an adjunct, the control system is also discussed in a top level fashion.

The retrieval of quantitative information of the atmosphere from lidar-return signals is know as lidar inversion and it requires solving the lidar equation for the constitutive optical parameters, namely, the attenuation (or extinction-coefficient) and the backscatter-coefficient. This is tackled in Chaps.7 and 8. The inversion algorithms presented are aimed only at the assessment of the primary optical parameters. Transmittivity (extinction) and backscatter measurements are meaningful in instances of visibility assessment in fog or hazes, ceilometry studies (cloud height extent) and qualitative mapping of particulate motion in the atmosphere, which is useful to derive tangential wind-speed. The more general problem of relating them to the physical factors of appropriate concern (for example: mass-concentration or particle size distribution of a pollutant source; temperature, pressure and humidity within an observation cell; etc.) constitutes a very breadth problem that would justify a stand-alone research work by itself.

In my opinion, the lidar inversion is in fact a two-fold problem and hence, I have preferred to classify the inversion algorithms into non-memory and memory ones. This depends on whether the algorithm performs pulse-to-pulse inversions with complete independence from past-retrieved information or not. The former kind of algorithms is studied in *Chapter 7*. On this subject there are very few available references, basically, the slope method of Kunz and Leeuw [187] and Klett's algorithm [186]. This chapter addresses the development of efficient non-memory algorithms as well as error assessment methods that enable to work out error inversion plots for each of the algorithms considered. Since no references exist on this subject, assessment of the sensitivity of each algorithm to the different input parameters, correlation hypotheses and system calibration, which very often involve large uncertainties, is also of prime concern.

Memory algorithms are studied in *Chapter 8* and they constitute a major research pole of this thesis since no references are known. As a brief outline, the atmosphere is modelled in a vector form so that for each cell in the lidar beam-path, attenuation and backscatter parameters are sought. The problem is formulated from the point of view of modern control theory and parameter estimation, which leads to the application on

XVIII Introduction.

nonlinear Kalman filtering and stochastic modelling of the atmosphere. Using these powerful tools, the algorithms presented will do their best to make the most from present and past information deduced from the return signal. Regarding the complexity of these algorithms and in order to somehow grade the filter, the inversions performed in this chapter have worked with synthesized raw-data, leaving for the next chapter their application to real data.

To sum up, the aftermath of the lidar system developed is treated in *Chapter 9*. Analysis and interpretation of the signals obtained through the lidar system are discussed. In addition, this chapter gives a deep insight into the kind of measurements carried out with our lidar and discusses as well the system performance in a real situation, comprising both day- and night-time operation. The demonstrated capabilities of the lidar, the problems limiting full realization of lidar's potential in atmospheric probing and beyond that, the future prospects of the lidar activity in the Department are presented in *Chapter 10*, where concluding remarks are exposed.

Although I have endeavored to be as comprehensive as possible, the possibilities of the designed lidar including the newest digital units designed with a view to a mobile motorized system are already so large that there are bound to be unexploited. For these I apologize.

CHAPTER 3 LINK-BUDGET AND SYSTEM SPECIFICATIONS

In this chapter, link-budget design equations and specifications of the lidar system are derived and discussed.

Setting off from the basic lidar equation, emphasis is given to the system optics trade-offs, basically, emitting laser and receiving telescope. Here, the design is further complicated by geometrical considerations that include the degree of overlap between the laser beam and the field-of-view of the receiver optics. Typical power levels, signal-to-noise ratio at the receiver's output and lidar range performance are also assessed. This involves evaluation of different photodiodes and system operation modes such as shot-noise limited, dark-noise limited and thermal-noise limited.

The interpretation and cross-examination of the great quantity of lidar parameters that play a role in the overall system performance has justified the development of a second software package, *link-budget*. The plots and computations presented have been worked out with it and include measured values whenever possible. In addition to the design equations, there are economical, technological and mechanical constraints that limit the scope of the equations derived. Other chapters of this thesis work will concentrate on the design and measurement steps of the devices involved.

1. LINK-BUDGET ORIENTED LIDAR EQUATIONS

1.1 The basic lidar equation

Since this project is concerned to the elastic interaction between the laser radiation and the atmosphere, where both incident and scattered radiation are at the same wavelength, the general form of the lidar equation [25] may formally be expressed in the following *single-scattering lidar equation* [9]:

$$P(\lambda,R) = P_o \left(\frac{c\tau_l}{2}\right) \beta(\lambda,R) \frac{A_r}{R^2} \exp\left[-2\int_0^R \alpha(\lambda,r) dr\right] \xi(\lambda) \xi(R)$$
 (1)

where:

 $P(\lambda,R)$ is the instantaneous received power from the range R and wavelength λ ,

 P_o is the transmitted power at time t_o ,

c is the speed of light,

 τ_l is the laser pulse duration,

 $\beta(\lambda, R)$ is the volume backscatter-coefficient of the atmosphere [m⁻¹·sr⁻¹] at wavelength λ over range R,

R is the range,

A, is the effective receiver area,

 $\alpha(\lambda, R)$ is the volume extinction-coefficient of the atmosphere [m⁻¹] at wavelength λ over range R,

 $\xi(\lambda)$ is the receiver's spectral transmission factor and,

 $\xi(R)$ is the overlap factor or geometrical form factor.

Before proceeding further, it is worth making some comments about the interpretation of the coefficients α and β in the lidar equation:

The volume extinction coefficient, α , is defined as the cross-section per unit volume $[m^2/m^3]$, and it is numerically identical to the linear extinction-coefficient used in laser propagation equations, which has units of $[m^{-1}]$. It also coincides with the extinction-coefficient introduced in Chap.2.

The volume backscatter-coefficient, β , is defined as the fractional amount of incident energy scattered per unit solid angle [sr] in the backward direction per unit atmospheric length. It agrees with the definition given in Chap.2 as the backscatter cross-section per unit volume and unit solid angle [m²/(m³·sr)].

Since the transmitted laser pulse has a finite duration τ_1 , it illuminates a finite geometrical length $c\tau_1$ of the atmosphere at any instant. However, since the received energy must travel a two-way path, the atmospheric length (or range increment) from which signals are received at any time t is just half this value. Thus, the distance

$$\Delta R = \frac{c \, \tau_l}{2} \tag{2}$$

is called the *effective pulse length*. It is exactly half of the actual length instantaneously illuminated by the pulse because of the two-way path that all received energy must traverse.

There are, however, other parameters of concern to the receiver and emitting optics. The effective receiver area A_r enters eq.(1) because it determines the solid angle

$$\Omega_o = \frac{A_r}{R^2}$$
 [sr]

subtended by the receiver at range R [26]. Provided that the angle of divergence of the transmitter beam does not exceed the angle of acceptance of the receiver, all the energy transmitted will be available for backscattering at range R. Otherwise overlap factor losses should be considered.

The expression

$$T(\lambda,R) = \exp\left[-2\int_{0}^{R} \alpha(\lambda,r) dr\right]$$
 (4)

represents the fractional transmittance of energy at wavelength λ along the two-way path between the lidar and range R. This depends upon α , the volume extinction coefficient of the atmosphere, which represents the fraction by which the flux of energy in the direction of propagation is reduced per unit length. From Chap.2, gases, aerosols and hydrometeors contribute to both absorption and scattering of energy. Formally,

$$\alpha = \alpha_{g,scat} + \alpha_{g,abs} + \alpha_{p,scat} + \alpha_{p,abs}$$
 (5)

where the subscript g means gases (Rayleigh's components, see Sect.2, Chap.2), p means particulate constituents (Mie's components, see Sect.3, Chap.2), abs means absorption and scat means scattered. Recall that $\alpha_{g,a}=0$ at the operating wavelengths of the lidar, $\lambda=532nm$ and 1064nm (Sect.1, Chap.2). Strictly speaking, the term α applies in this simple form only when Bouguer's law (the extinction law) is valid, that is, when essentially all the scattered energy is permanently removed from the outgoing lidar beam. In strongly scattering atmospheres (e.g. clouds, thick hazes, fog) multiple scattering occurs, and corrections must be made to eq.(1).

Alternatively, the lidar equation may be formulated in terms of the emitted energy noting that [25]

$$P(\lambda,R) = \frac{E(\lambda,R)}{\tau_d}$$
; $P_o = \frac{E_l}{\tau_l}$ (6)

where

 $P(\lambda,R)$ is the range-received power at wavelength λ ,

 $E(\lambda, R)$ is the range-received energy at wavelength λ ,

 P_o is the laser transmitted power at time t_o ,

 E_l is the laser pulse energy,

 τ_I is the laser pulse duration and,

 au_d is the sampling time or integration period of the detector.

It becomes:

$$E(\lambda, R) = E_l \frac{c\tau_d}{2} \beta(\lambda, R) \frac{A_r}{R^2} T(\lambda, R) \xi(\lambda) \xi(R)$$
 (7)

Finally, the terms $\xi(\lambda)$, $\xi(R)$ represent the receiver's optical losses. Thus, the first one, represents the receiver's spectral transmission including any spectrally selecting elements such as filters or monochromators. Because of the high degree of monochromaticity of the laser energy, extraneous light can be excluded to a substantial degree by the use of a narrow band filter centered on the laser wavelength. Basically, such light will come from the background radiation (some figures were estimated at the operating wavelengths by *link-atmos* in Sect.5, Chap.2 and are reproduced here in Tab.1). The increment of radiative background power accepted by the receiving optics can be expressed in the form [26]

$$P_{back} = L_b(\lambda) A_r \Omega_r d\lambda \qquad [W]$$

where

 $L_b(\lambda)$ represents the spectral radiance of the sky background [W·m⁻²· μ m·sr⁻¹],

 A_r is the receiver-system effective aperture [m²]

 Ω_r is receiver-system acceptance solid angle (eq.(3)) [sr]

 $d\lambda$ is the equivalent spectral width of the spectrally selecting component (e.g. filter) [μ m].

Note that the term P_{back} represents the incident background power within the optical bandwidth and hence the receiver-system transmission efficiency $(\xi(\lambda), \xi(R))$ is computed separately (eq.(1)). In other words, P_{back} is only affected by the factor $\xi(\lambda)$.

The second term or *overlap factor*, $\xi(R)$, depends only upon the overlap of the area of laser irradiation (spot at range R) with the field of view of the receiver optics. Incidentally, because laser energy can be highly collimated, it would be desirable to direct all the transmitted energy into a narrow beam and restrict the field of view of the telescope to this angle, thus minimizing background light entering the system. The measured divergence is about $0.1 \, mrad$ for the Nd:YAG laser used but typical values may also reach 2 or 3 mrad. In the following chapters, this point will be reconsidered since the election of our photodiode may severely limit the field-of-view.

1.2 Simple overlap factor

The geometrical form factor for a coaxial lidar having no apertures (other than the objective lens or mirror of the telescope) or obstructions is unity, provided the divergence angle of the laser beam is less than the opening angle of the telescope.

The geometrical form factor can be evaluated fairly easily for a biaxial lidar (Fig.1), as the present case is, if the objective lens of the telescope represents the limiting aperture of the receiver optics, any obstruction is neglected, and an uniform laser distribution over the area of illumination is assumed.

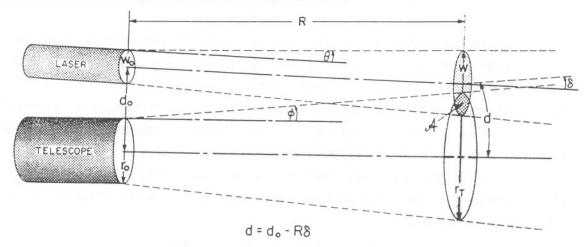


Fig. 1 Geometry of the biaxial lidar of the UPC [25].

Under the conditions of Fig.1 one can think of $\xi(R)$ as a simple overlap factor, and one can write [25]

$$\xi(R) = \frac{A\{r_T(R), W(R); d(R)\}}{\pi W^2(R)}$$
 (9)

where A represents the area overlap function, $r_T(R)$, the radius of the radius of the receiver-optics field of view in the target plane at range R, and W(R) the radius of the circular region of laser illumination or spot at range R. In formulating these equations, the field of view of the receiver optics in the target plane is assumed a circle of radius

$$r_{\tau}(R) = r_o + \phi R \tag{10}$$

where

 r_0 represents the effective radius of the telescope lens (or mirror); and

 ϕ represents the receiver-optics half opening angle.

As for the laser beam radius, assuming the output of the laser is predominantly in the TEM_{00} mode, one can write [33][36]

$$W(R) = \{W_o^2 + \theta^2 R^2\}^{1/2}$$
 (11)

where

 W_o represents the laser output aperture radius; and

 θ represents the laser's half divergence angle.

The separation of the telescope and laser axes in the target plane is

$$d = |d_o - R\delta| \tag{12}$$

where

 d_{o} represents the separation of the axes at the lidar, and

 δ represents the inclination angle between the laser and the telescope axes (see Fig.1).

These variables are indicated in Fig.1 along with the laser divergence half angle θ and the telescope half angle field-of-view ϕ . Thus, if a circular detector of radius r_D is positioned on the axis of the telescope of effective focal length f, then [26]

$$\phi = \frac{r_D}{f} \tag{13}$$

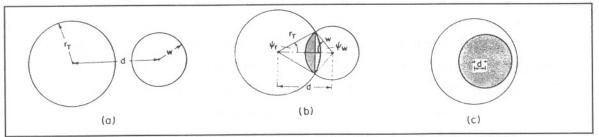


Fig. 2 Three overlap situations possible for a biaxial lidar [25].

With regard to Fig.2, three situations are possible:

1. The separation of the axes is too large for there to be any overlap area between the receiver-optics field-of-view and the area of laser illumination (Fig. 2a). Then,

$$A = 0 if d > r_T + W (14)$$

2. The separation of the axes is small enough that either the area of laser illumination lies totally within the receiver-optics field of view or vice versa. The former case is illustrated in (Fig.2c) and would correspond to an overlap factor equal to unity. This amounts to saying that if

$$d < |r_{\tau} - W| \tag{15}$$

then the overlap factor may be computed as the ratio of areas

$$\xi(R) = \frac{\pi r_T^2(R)}{\pi W^2(R)} \approx \left(\frac{\phi}{\theta}\right)^2$$
 (16)

3. The separation of the axes lies between these extremes (Fig. 2b):

$$|r_T - W| < d < r_T + W \tag{17}$$

Under these circumstances the are overlap function is

$$A\{r_T, W; d\} = W^2 \psi_W + r_T^2 \psi_r - r_T d \sin \psi_r$$
 (18)

where

$$\psi_W = \cos^{-1} \left[\frac{d^2 + W^2 - r_T^2}{2Wd} \right] \qquad \psi_r = \cos^{-1} \left[\frac{d^2 + r_T^2 - W^2}{2r_T d} \right]$$
 (19)

It is customary to define the normalized range z, and other dimensionless parameters as follows:

$$z = \frac{R}{r_o}, \qquad A = \frac{r_o}{W_o}, \qquad D = \frac{d_o}{r_o} \tag{20}$$

Based on the normalized range z, the behaviour of $\xi(z)$ in the case of a biaxial lidar with an inclination δ between the telescope and laser axes is depicted in Fig.3.

In this case $\xi(z)$ increases with z at first, attains the value of unity over some range interval, and then rapidly drops to zero for larger values of z. This is illustrated in Fig.3, where $\xi(z)$ is plotted against z for three values of the inclination angle ($\delta=0.05, 0.01, and 0.001 \ rad$) and two values of A (5 and 20). In this set of examples, D=1.25 and $\theta=\phi=1 \ mrad$, which correspond to typical values in lidar systems.

Besides Fig.3, Fig.4 depicts the overlap factor for the inclinations $\delta = 0$, 1 and 2 mrad and the telescope and laser defaults of Tab.1. (Range is not normalized).

These results clearly indicate that interpretation of short-range lidar measurements must take proper account of the overlap factor to compensate the range-received power. Otherwise, $\xi(z)$ may lead to misinterpretation of the measurements by the inversion algorithms. Misalignment of the telescope and laser axes is extremely critical. Thus, simulation using the same default values for D, θ and ϕ have shown that misalignment of only 10 mrad would lead to a lack of signal return for z > 300 (i.e., $R > 300r_o$).

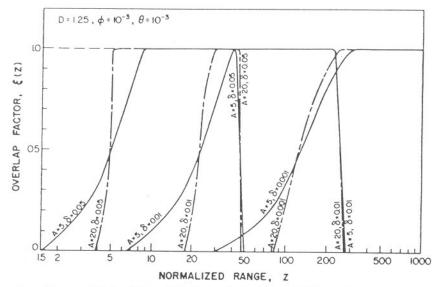


Fig. 3 Overlap factor $\xi(z)$ with z (A=5 and 20, δ =0.001, 0.01, and 0.05 rad) [25].

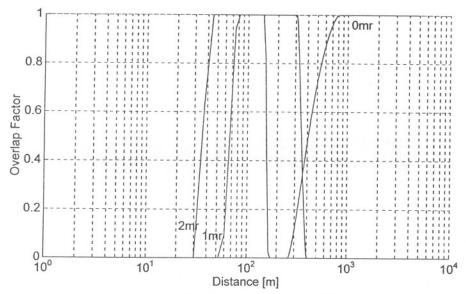


Fig. 4 Overlap factor $\xi(R)$ with R ($d_o=18$ cm and $\delta=0$, 1 and 2 mrad) (Tab. 1).

1.3 The visibility margin approach

Two factors in eq.(1), the elastic volume backscatter-coefficient β , and the attenuation (or extinction) coefficient α determine the lidar signal strength.

The visibility margin concept along with Fig.5 from [9] have been used to obtain lidar performance estimates under various meteorological conditions. Homogeneous atmosphere is assumed [9][25]. The figure shows typical values of β and α for a range of wavelengths and atmospheric conditions. These values have been corroborated using Mie's models and the procedures introduced in Chap.2.

Strictly speaking, the *visibility margin* term is defined under nonturbid atmospheric conditions. That is, one which is free of aerosol particles. Then, the total attenuation of laser radiation is defined by its molecular extinction. The Koshmieder's relation connects

the meteorological visibility V_M with the extinction-coefficient. It is usually given for the wavelength of $0.55\mu m$ (maximum sensitivity of the human eye [9]). Kruse et al. [25] gave a more general relation for any wavelength λ

$$\overline{\alpha_{\lambda}} = \frac{3.912}{V_M} \left(\frac{550}{\lambda}\right)^q \quad [km^{-1}] \qquad q = \begin{cases} 0.585 V_M^{1/3} & V_M \le 6km \\ 1.3 & otherwise \end{cases}$$
 (21)

The case q=1.3 represents average seeing conditions. Expected mean extinction, backscatter and visibility margins are shown decadically spaced in Fig.5, where eq.(21) has even been applied to quite turbid atmospheres such as dense water clouds.

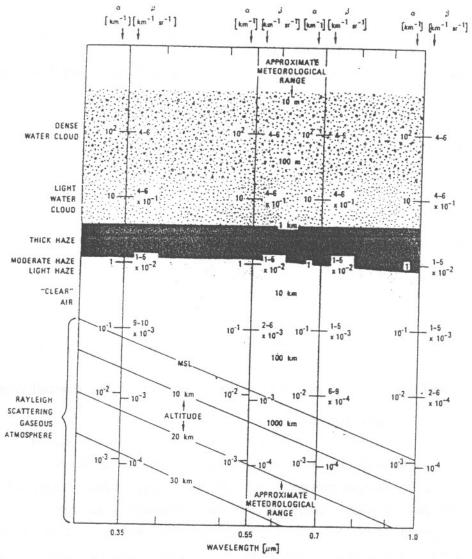


Fig. 5 Estimation of extinction, backscatter and visibility margin variation with atmospheric condition used in link-budget studies [9].

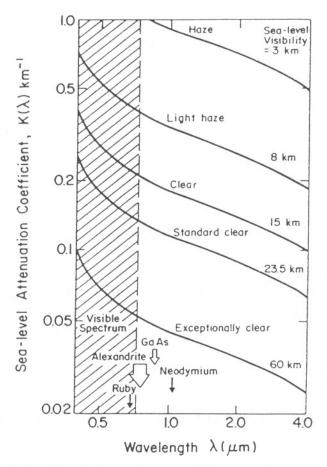


Fig. 6 Sea-level attenuation coefficient $\alpha(\lambda)$ vs. visibility [25].

Fig.6 shows the same concept from another source (Pressley, [25]). Note that more optimistic values are shown.

1.4 Design comments and default values concerning this section

Fig. 7 and Fig. 8 illustrate range-received power for the visibility margins indicated (values are logspaced) according to the defaults of Tab.1. It includes two situations: in one case, the laser output energy is 500 mJ (λ =532 nm) and in the other 1 J (λ =1064 nm).

From the beginning, a design goal was to choose a photodiode that could either work as PIN and as avalanche photodiode (APD). In addition, it should have acceptable responsivities at both operating wavelengths of the lidar system (1064 and 532 nm). The selection steps led to the EG&G C30954E photodiode.

This criterion has justified the sacrifice of *overlap-factor* considerations in favour of versatility. Another important drawback is the difficult manoeuvrability of the laser. This has conditioned different set-ups for the lidar system that will be discussed in detail along the experimental chapters of this work. For the time being, overlap factor losses have been neglected in Fig.7 and Fig.8 and assume $\xi(\propto)=1$ as shown in Tab.1.

OPTICAL PARAMETERS

Laser parameters: [118]

Energy: $E_{1,1} = 500 \text{mJ} \ (\lambda_1 = 532 \text{ nm})$

 $E_{1.2} = 1J (\lambda_2 = 1064 \text{ nm})$

Divergence:

 $\theta = 0.1 \text{ mrad}$

Pulse length:

 $\tau_1 = 7-10 \text{ ns}$

Waist: $W_0 = 1$ cm

Receiving optics:

a) Telescope:

focal length:

f=2 m

aperture:

ø20 cm

transmittance: 60

60 % (includes photodiode window)

field-of-view $\phi(eq.(13))$:

 ϕ =0.2 mrad (photodiode \emptyset 0.8 mm)

b) Filters [117]:

bandwidth:

 $\Delta \lambda = 10 \text{ nm}$

transmittance:

50 % (at both wavelengths)

Lidar equation parameters (eq. (7))

Net losses:

 $\xi(\lambda) = 0.3$

(at both wavelengths)

Overlap factor (eq.(16)):

 $\xi(\propto)=1$

(if $|\delta| < \theta + \phi$)

Estimated background radiance:

 $L_{\text{back}}(\lambda_1) = 48.86 \text{ W} \cdot \text{m}^{-2} \cdot \mu \text{m}^{-1} \cdot \text{sr}^{-1}$

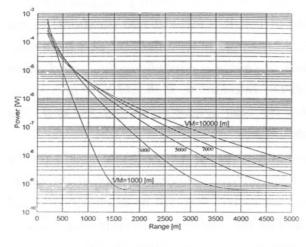
 $(Worst-case\ {\it global}\ {\it radiance}\ assessment\ with\ {\it link-atmos}\ modelling\ software.$

April 15th, 15:00 GMT, telescope's elevation 90°)

Tab.1 Defaults used in link-budget simulations of Sect.1

As for the background power, there has been assumed the one that will be collected by a vertically aimed telescope under the worst day and hour in April.

Fig. 7 and Fig. 8 are parameterized for the set of visibility margins ($V_M = 1$, 3, 5, 7 and 10 km). The design has been worked out with these meteorological ranges.



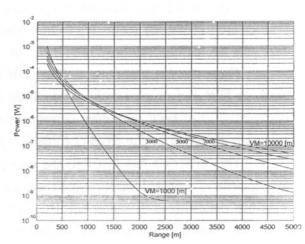


Fig. 7 Range-received power $(E_I = 500mJ)$

Fig. 8 Range-received power ($E_2 = 1J$).

2. SIGNAL-TO-NOISE RATIO ASSESSMENT IN THE LIDAR RECEIVER

An APD/amplifier combination will be used to detect the faint return of the scattered lidar pulse. Receiver bandwidth, B, is typically designed so that $B \approx 0.35/\tau_d$ [149]. Yet, for optimal timing resolution of the return pulse, higher bandwidths as large as $B \approx 0.5/\tau_d$ according to the Nyquist criterion are used. SNR depends on the collecting optics and receiver combination. For optimum SNR, a design/cost compromise must be struck between good optics (low f-number), detector diameter and preamplifier type.

This section focus on the receiver's SNR itself. On the one hand, noise sources in the photodetector along with its intrinsic parameters are reviewed in Sect.2.1. The transimpedance amplifier (TIA) will carry out the current-to-voltage conversion of the signal delivered by the photodiode. After that, several stages of amplification will bring the signal amplitude to the level required for further signal processing (such as inversion of the optical parameters, extinction and backscatter) in a computer. In order to characterize the lidar receiver (TIA stage in the simplest case), noise sources due to subsequent amplification and conditioning stages will be considered in terms of their equivalent thermal noise variances.

On the other hand, signal-to-noise ratio of the whole lidar receiver will be evaluated in Sect. 2.2.

2.1 Noise statistics for an APD-amplifier module

The probability of photoelectric conversion of an incident photon; (or *quantum* efficiency η) in the APD is a function of its wavelength. About 1100 nm, photons do not possess enough energy to promote silicon valence electrons across the bandgap to the conduction band. Below 1100 nm, photons of different wavelengths will be absorbed at various mean depths in the APD, depending on the semiconductor's absorption coefficient. Reference [153] provides an excellent insight into semiconductor physics. To improve efficiency, antireflective coatings are evaporated on the diode front surface. By selecting the optical thickness of this layer, quantum efficiency curves are enhanced in the spectral regions of interest [136]. The decisive features of APDs as compared to photomultiplier tubes (PMTs) are reduced price and higher quantum efficiency over a broader spectrum that any PMT [136][122]. For APDs, high gain in linear mode comes from applying a high reverse bias voltage which in turn creates a wide avalanche region around the junction of the semiconductor. For PIN photodiodes, there is not such multiplication [145][147].

The current (intensity) responsivity R_i , quantifies the photoelectric gain of a photoelectror. It directly depends on the quantum efficiency and it is expressed as

$$R_i = \eta \frac{q\lambda}{hc} M = \frac{\eta \lambda}{1.24 \cdot 10^{-6}} M \qquad \left[\frac{A}{W} \right]$$
 (22)

where

c is the speed of light,

q is the electron charge,

 λ is the wavelength of the incident photons,

h is the Planck's constant,

M is the multiplication factor. (M=1 for PIN photodiodes).

Very often, the current responsivity is expressed terms of the intrinsic responsivity of the APD. It is the one the APD would have if it had no gain (PIN mode, M=1)

$$R_{io} = \eta \frac{q \lambda}{h c} \rightarrow R_i = R_{io} M \tag{23}$$

If the average number of incident photons on the APD for a time τ_d is k, the average number of photons (after multiplication) is $\mu = M\eta k$. Photoelectron conversions are ruled by Poisson statistics and hence, mean and variance coincide. Yet, as this variance derives from the random fluctuations in the number of carriers generated, the excess noise factor, F, takes into account the randomness of the multiplying phenomenon giving $\sigma^2 = FM^2\eta k$ [123].

To these electrons, there also add those giving rise to the dark current, whose statistics are also poissonian and whose mean and variance are given by

$$\begin{cases}
\mu = (I_{ds} + MI_{db}) \frac{\tau_d}{q} \\
\sigma^2 = (I_{ds} + FM^2 I_{db}) \frac{\tau_d}{q}
\end{cases}$$
(24)

where

 I_{ds} is the APD's surface dark current,

 I_{db} is the APD's bulk dark current and the other terms have already been defined.

P-I-N or other types of junctions of a photodiode does not present an infinite resistance to reverse current flow. Consequently, when a reverse bias is applied to a photodiode, a small current flows even in the absence of incident light. This dark current I_d , increases slowly with increasing reverse bias. For an APD, bulk leakage current, I_{db} , is multiplied by the gain, M. Therefore, dark current I_d equals

$$I_d = I_{ds} + MI_{db} \tag{25}$$

Contrary to what happens with VAPDs or PMTs [136] that are ideal for single photon counting (e.g. low light spectroscopy [128]), one may well assume that the count numbers are high enough for APDs. In such case, discrete Poisson statistics may be approximated by continuous, gaussian ones. Noting that the *electron count* random variable is related to the *APD output current* random variable by means of the factor q/τ_d and that the photocurrent and dark current processes are independent, the following expressions for the mean and variance current follow:

$$\begin{cases} \mu_{i} = \frac{q}{\tau_{d}} M \eta \, k + (I_{ds} + M I_{db}) \\ \sigma_{i}^{2} = \left(\frac{q}{\tau_{d}}\right)^{2} M^{2} F \eta \, k + \frac{q}{\tau_{d}} (I_{ds} + F M^{2} I_{db}) \end{cases}$$
(26)

Usually, these expressions are rewritten in terms of the current responsivity R_i (eq.(22)), the optical input power P and over I Hz bandwidth [20] noting that

$$B = \frac{1}{2\tau_d} \qquad [Hz] \tag{27}$$

If one introduces the optical power P_s , the current mean and variance become

$$\begin{cases} \mu_i = R_i P_s + (I_{ds} + MI_{db}) & [A] \\ \sigma_i^2 = 2R_i^2 \frac{hc}{\eta \lambda} F P_s + 2q(I_{ds} + FM^2 I_{db}) & \left[\frac{A^2}{Hz} \right] \end{cases}$$
(28)

Now, that both current mean and variance are have been formulated, it is worth defining the *Noise Equivalent Power (NEP) [107]*. It is defined as the incident light level impinging on a photodiode, which produces a photocurrent equal to the noise level. It is usually regarded as the most significant figure of merit for a photodetector. The NEP is a function of the photodiode's responsivity (and hence, of the wavelength λ) and the noise of the photodiode (eq.(24)). In system applications whose SNR dominated by the photodiode performance (no thermal noise dominant), the SNR may be computed by taking the ratio of the incident optical power to the photodiode NEP.

In general terms, using eqs.(28) and (23), NEP is defined as follows:

$$NEP(\lambda, T) = \frac{\sigma_d}{R_i} = \frac{[2q(I_{ds} + FM^2I_{db})]^{1/2}}{\frac{\eta q\lambda}{hc}M} \qquad \left[\frac{W}{Hz^{1/2}}\right]$$
(29)

The nomenclature NEP(λ ,T) indicates wavelength λ , and temperature, T dependence.

One step further, after multiplication by the TIA gain, G_T , the optical-to-voltage conversion can be quantified by introducing the *voltage responsivity* (see also eq.(22))

$$R_{v} = R_{i}G_{T} = \eta \frac{q\lambda}{hc}MG_{T}$$
 (30)

Finally, inclusion of the equivalent thermal noise variance σ_{th}^2 [V²/Hz] of the preamplifier enables to express the mean and variance components of the output voltage in terms of the voltage responsivity. They become [127]

$$\begin{cases} \mu_{v} = R_{v}P_{s} + G_{T}(I_{ds} + MI_{db}) & [V] \\ \sigma_{v}^{2} = 2R_{v}^{2}\frac{hc}{\eta\lambda}FP_{s} + 2qG_{T}^{2}(I_{ds} + FM^{2}I_{db}) + \sigma_{th}^{2} & \left[\frac{V^{2}}{Hz}\right] \end{cases}$$
(31)

But for the amplifier noise, it can be seen from eq.(31) that the main sources of noise in the APD are shot noises, and originate from the primary photocurrent (noise in signal) and the dark current (rms dark noise). By blending eqs.(31) and (23), the signal, P_s , and dark bulk current, I_{db} , evidence a similar contribution to the shot noise variance

$$\begin{cases} \sigma_{sh,s}^2 = 2qG_T^2FM^2R_{io}P_s & \left[\frac{V^2}{Hz}\right] \\ \sigma_{sh,d}^2 = 2qG_T^2(I_{ds} + FM^2I_{db}) & \left[\frac{V^2}{Hz}\right] \end{cases}$$
(32)

where subscripts sh, s, d mean shot, signal and dark, respectively.

Two important points emerge from this equation: One is that both the power signal and the dark bulk current contribute to the shot noise exactly alike. Another is that APD noise performance is degraded by the excess noise factor, F. This parameter measures the variation in gain of both photocurrent and noise current introduced during multiplication. It can be computed using the model developed by McIntyre [148], which considers the statistical nature of the avalanche multiplication. Thus,

$$F(M) = kM + \left(2 - \frac{1}{M}\right)(1 - k)$$
 (33)

where k is the ionization ratio (ratio of hole to electron ionization probabilities [153]) and,

M is the APD gain factor.

It should be noted that these expressions can be used for PIN photodiodes by taking M=1, F=1. Fig. 9 illustrates excess-noise factor behaviour vs. M.

2.2 Signal-to-noise ratio of the lidar receiver

Noise is computed in terms of the equivalent receiver system noise, B, at the TIA output. This bandwidth corresponds to the sharpest filter of the receiving chain (the antialiasing filter of the lidar receiver).

Equivalently, SNR can be calculated at the TIA output by defining the noise equivalent voltage density at its output, σ_{th} . It blends both the thermal noise of the TIA and that of the subsequent amplification stages (e.g. conditioning amplifiers and sampling card).

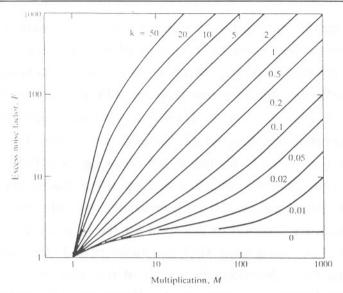


Fig. 9 Excess-noise factor calculated from eq. (33) and [20].

In the lidar receiver the signal term, P_{s_s} blends both the range-receiver lidar signal P(R) and the background power P_{back} (Chap.2). Formally,

$$P_{s} = LP(R) + \xi(\lambda)P_{hack}$$
(34)

where $L(\lambda, R)$ represents the optical losses (Sect. 1.4), for any range R, and wavelength, λ

$$L(\lambda, R) = \xi(\lambda)\xi(R) \tag{35}$$

The SNR can easily be computed by considering the mean voltage term in eq.(31) that contributes to the signal along with (32) and (34). It yields:

$$\frac{S}{N} = \frac{R_{v}LP(R)}{\left\{2qG_{T}^{2}[I_{ds} + FM^{2}(I_{db} + R_{io}[LP(R) + \xi(\lambda)P_{back}])]B + \sigma_{th}^{2}B\right\}^{\frac{1}{2}}}$$
 [V] (36)

Signal-induced shot noise, dark current shot noise and thermal noise can be rewritten as

$$\begin{cases} N_{sh,s} = \sigma_{sh,s}^{2} B = 2q G_{T}^{2} F M^{2} R_{io} [L P(R) + \xi(\lambda) P_{back}] B & [V^{2}] \\ N_{sh,d} = \sigma_{sh,d}^{2} B = 2q G_{T}^{2} (I_{ds} + F M^{2} I_{db}) B & [V^{2}] \\ N_{th} = \sigma_{th}^{2} B & [V^{2}] \end{cases}$$
(37)

where the subscripts sh, th, s, d mean shot, thermal, signal and dark, respectively.

2.3 Choosing the right detector

Obviously, one of the key parameters that has to be considered when choosing an APD for the lidar receiver is noise performance [145]. Like other detectors, an APD will be operating in one of two noise-limited detection regimes. Sensitivity (or minimum detectable power) will be limited by dark-current shot noise or preamplifier's thermal

noise. Regarding eq.(36), since the lidar signal is a range-dependent signal, this will always be the case at long ranges, where the return signal is weaker. As seen in Sect.2.1, APD noise performance is degraded by an excess noise factor, F, and hence SNR at high power levels for and APD detector is worse than for PIN detector with the same quantum efficiency. This is illustrated in Fig.10. There, the behaviour of the APD C30954 of EG&G Optoelectronics is simulated for different multiplication factors. The case M=1 illustrates the behaviour of this versatile photodetector, working as a PIN photodiode. (A PIN detector with the same quantum efficiency would perform exactly like this APD with unity gain). The graphs assume that the test has been carried out with a transimpedance amplifier whose specifications are identical to that used for the lidar receiver front-end. They are listed in Tab.2 (p.3.26) along with APD specifications and other simulation parameters.

In fact, the range-dependent behaviour of the lidar signal, would condition the multiplication gain, M, to the exploring range. Of course, a criterion would be to somehow switch from PIN to APD mode at certain long range. Let us consider this hypothetical situation and assume a typical lidar range of 5 km. If so, the lidar signal would last for $33 \text{ } \mu s$. In addition, if the maximum gain is about M=400 for a reverse polarization of $V_R=400 \text{ V}$, and M=1 is achieved at $V_R=15 \text{ V}$, the high voltage source (HVS) would have to undergo a voltage swing of $385 \text{ V in only } 33 \text{ } \mu s$, every lidar shot. Obviously, this option is not possible, as seldom do HVS settling times fall below a few tenths of a second.

Evident in the curves of Fig.10 is the *knee* where SNR becomes limited by signal shot noise. Noise variances in eq.(32) (equivalently eq.(37)) are illustrated in Fig.11. Note that the intersect-point between signal-induced shot noise and thermal noise variances coincides with the *knee* in Fig.10. In the *knee* the photodiode changes from a signal shotnoise limited regime to a thermal-noise limited one.

All considered, the above controversy between choosing an APD or a PIN photodiode has been solved in favour of an APD C30954E of EG&G Optoelectronics. These are the most important pros:

- 1) From the beginning, a device with acceptable quantum efficiency at both wavelengths (1064 and 532 nm) was wished. This constraint reduced the number of possibilities very much. For this APD, typical responsivities as a function of the wavelength λ are:
 - $R_i(\lambda = 532nm) = 30.8 \pm 0.5 \ A/W$ $R_i(\lambda = 1064nm) = 33.6 \pm 0.6 \ A/W$ (Figures from the device data sheets at multiplication gain M = 120).
- 2) Depending on the bias voltage, the *photodetector can work either as a PIN* (M=1) or as an APD (M>1). Therefore, a single device can cope with short and long range explorations by adjusting the optimum multiplication gain M.

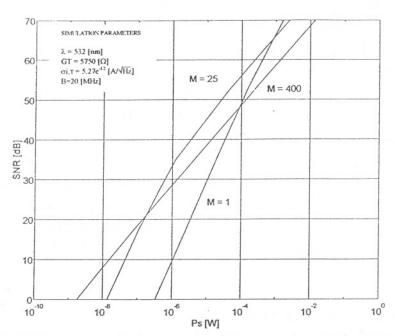


Fig. 10 SNR versus optical power for different gains (APD C30954E).

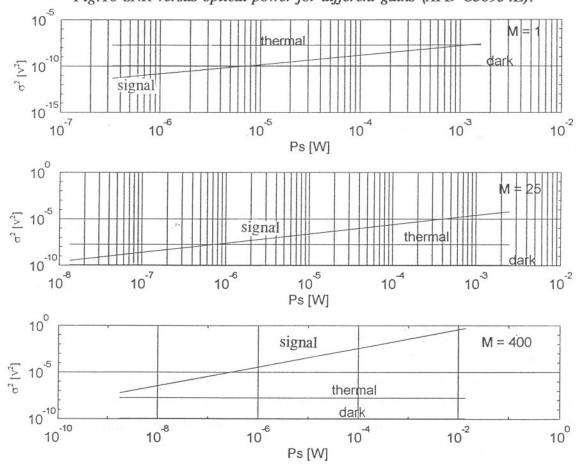


Fig.11 Noise variances for the APD EG&G C30954E.

- 3) APDs are cheaper and more robust than photomultiplier tubes (PMT).
- 4) Such versatile photodetector represents a *sensible choice between PIN and PMT or VAPD [136] solutions*.

And this is the major con to tackle:

1) The field-of-view of the telescope is severely reduced (see Tab.1) considering the small diameter (0.8 mm) of the APD. Thus, the use of a mirror to direct the laser beam to the atmosphere is a feasible solution that guarantees no overlap factor losses (eq.(16)). Otherwise, if light is output by means of a high power fiber optic coupled to some adaptation optics, overlap factor losses can be very large. This suggests the possibility of designing a second telescope with much lower focal length. That would enlarge the field-of-view of the telescope, according to eq.(13).

2.4 Noise limited modes and SNR

Dividing both numerator and denominator of eq. (36) by $R_{\nu}L_{\nu}$, yields

$$\frac{S}{N} = \frac{P(R)}{\left\{ \frac{2qI_{ds}}{R_{io}^{2}L^{2}} \frac{B}{M^{2}} + \frac{2qB}{R_{io}^{2}L^{2}} F(M) \left(I_{db} + R_{io} [LP(R) + \xi(\lambda)P_{back}] \right) + \frac{\sigma_{th}^{2}B}{R_{io}^{2}M^{2}G_{T}^{2}L^{2}} \right\}^{\frac{1}{2}} (38)$$

From here, four limiting situations arise [25]: The first regime or *signal shot-noise limited mode* occurs when noise due to the primary photocurrent becomes dominant. Then, eq.(38) tends to:

$$\frac{S}{N} \rightarrow \left(\frac{R_{io}L}{2\,qBF(M)}\right)^{\frac{1}{2}} P(R)^{\frac{1}{2}} \tag{39}$$

In this case, the highest sensitivity is achieved since the detectable signal is limited only by the quantum fluctuation of the signal itself. Note that SNR depends on the optical power as $P(R)^{1/2}$ rather than as P(R) and hence SNR degrades slower. In Fig.12 this situation occurs during the first part of the lidar exploring range and cannot be guaranteed when larger R_{min} are wished.

The second noise limited regime usually arises in daytime operation. Then, the level of background radiation can be so high that P_{back} is much higher that the lidar return. Under these circumstances one speaks of the *background-noise limited mode*. Using eqs.(38) and (8) the SNR becomes:

$$\frac{S}{N} \rightarrow \left(\frac{R_{io}L\xi(R)}{2qBF(M)P_{back}}\right)^{\frac{1}{2}}P(R) = \left(\frac{R_{io}}{2qBF(M)L_b(\lambda)A_r\Omega_o}\right)^{\frac{1}{2}}\left(\frac{\xi(\lambda)}{d\lambda}\right)^{\frac{1}{2}}\xi(R)P(R)$$
(40)

and it is evident that the filter system function $\xi(\lambda)$ and its bandwidth $d\lambda$ play an important role in assessment of the minimum detectable power.

The third case corresponds to the *dark-current-limited mode*. Assuming a photodiode gain $M \ge 10$, the surface dark current becomes less than 1 % of its bulk counterpart. This leads to an asymptotic SNR given by

$$\frac{S}{N} \rightarrow \left(\frac{R_{io}^2 L^2}{2qBF(M)I_{db}}\right)^{\frac{1}{2}} P(R) \tag{41}$$

Otherwise, a more complicated expression depending on both I_{ds} and I_{db} is obtained without further significative results.

Finally, the fourth case corresponds to the *thermal-noise limited mode*, the reader may feel more familiar with

$$\frac{S}{N} \to \left(\frac{R_{\nu}L}{\sigma_{th}\sqrt{B}}\right) P(R) \tag{42}$$

This situation is clearly identified in Fig.10 at intervals where the illuminating optical power is lower. Likewise, this behaviour is little by little identified in the lidar system SNR simulation of Fig.12 as long as the range increases. For different visibility margins, all the graphs become parallel ruled by the P(R) dependency.

As far as the multiplication factor (M) is concerned, two different behaviour arise once these four situations are considered: Since avalanche noise fluctuations or excess noise, F, monotonically increases with M (eq. (33)), rising M will only contribute to lower SNR in all shot-limited situations (signal-induced, background-induced, dark-induced). In a thermal-limited situation, increasing M will enhance SNR since the extra gain isolates the photodetector from the subsequent noisy stages.

2.5 The lidar receiver and signal-to-noise ratio enhancement

2.5.1. Philosophy of the lidar receiver

For the lidar system into consideration, the goal is to maximize system range. Based on Fig.12, SNR decreases with range. At long ranges, low light levels in the return-signal justify working in the APD mode, while at short ranges, high optical levels justify the PIN mode. *Eq.* (38) enables to formulate the lidar reception problem:

Given the laser output energy, E, and the minimum exploration range, $R_{min,}$ it is wished to:

- 1) find the optimum multiplication factor, M, that maximizes SNR at maximum exploration range, R_{max} , constrained to
- 2) the receiver's equivalent gain, G, that guarantees no saturation of the system. These two variables, M and G, define the M-G domain.

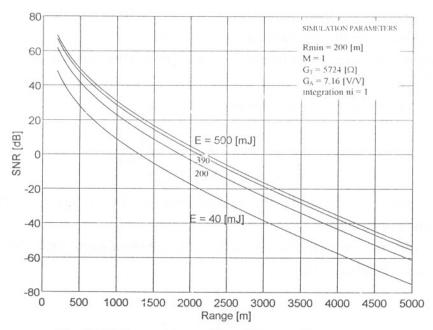


Fig. 12 SNR vs. range. ($\lambda = 532$ nm, $V_{\rm M} = 5$ km)

Maximum exploration range is ultimately determined by the dynamic range of the acquisition card. Since the data interval recorded will be $[R_{min}, R_{max}]$ and SNR(R) decreases with increasing range, it is wished to optimize the SNR at the maximum range.

The equivalent gain of the lidar receiving chain should provide adequate conditioning of the lidar signal into the full dynamic range of the acquisition card. In order to do this, the return-power samples from the minimum exploration range, R_{\min} , should be translated into the highest level of the acquisition card (or quite close to), while the lowest level would correspond to the absence of optical power detected.

If a $\pm V_{sat}$ bipolar card is used, the lidar receiver should ultimately perform the following conversion:

$$P(R_{min}) \rightarrow 2Vsat$$
 and no optical power $\rightarrow 0$

To achieve this final conversion, these voltage levels will have to be presented to the acquisition card with a $-V_{sat}$ offset. Even in situations where the background noise P_{back} may be neglected, samples from $R \to \infty$ will excite the lowest levels of the sampling card due to the thermal noise of the system. If one thinks in terms of equivalent noise power, this means both positive and negative spikes. So, if level translation were performed as stated, negative noise spikes would be clipped and, consequently, pulse integration would fail. This difficulty can easily be overcome by setting V_{sat} a bit lower than it should be (e.g. 5 % lower). Simulation of the AD converter with typical lidar signals, have shown that if noise is quantized with 3-4 bits, there will not be integration problems at all. This means 16 levels of the acquisition card, and an effective dynamic range of 8 bits (256). Of course, it greatly depends on the SNR at range of interest. Hence, one can summarize two important specs of the lidar receiver:

- a) The receiver has to be dc-coupled and must provide a variable offset with a low temperature drift. This offset should approximately be $-V_{sat}$ and adjusted during the training sequence of the lidar equipment.
- b) Receiver synchronization would be desirable in order to enable the receiver at $R_{min.}$ This would avoid deep saturation of the receiver and acquisition system during the interval $(0, R_{min})$.

Fig.13 illustrates the basic block diagram of the lidar receiver. In the figure, the goal (a) is accomplished using two amplification stages: The first stage, consists on a transimpedance amplifier that performs the basic current-to-voltage conversion. The second stage is basically a conditioning amplifier. This voltage-to-voltage amplifier provides extra gain and offset to meet the dynamic range specifications of the acquisition card $(\pm V_{sat})$. In fact, this is the simplest design one can think of to meet point (a) above.

Fig. 14 depicts basic noise sources in the lidar receiver under consideration.

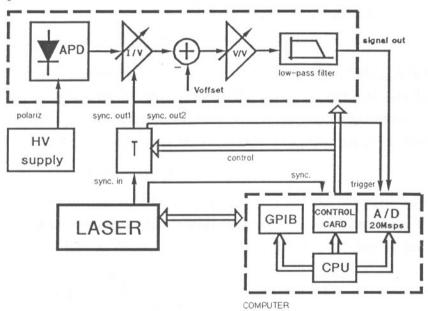


Fig. 13 Block diagram of the lidar system receiver.

Now that a rough schematic of the lidar receiver has been introduced, one can return to the initial problem of the M-G domain. Obviously, based on Fig.13, it is wished to obtain the values (M, G_T, G_A) that fulfil the requirements (1) and (2), that is, maximum signal-to-noise ratio at R_{max} and no saturation of the system. The latter point, implies neither saturation of the acquisition card, nor saturation of any amplifier of the receiving chain.

Since these goals require a more involved formulation, the problem will be solved in two steps for clarity reasons: In the first step, the receiving chain is assumed to be formed by the transimpedance amplifier followed by the acquisition card (Sect. 2.5.2). In the second step, the receiving chain, as sketched in Fig. 13 will be discussed in Sect. 2.5.3.

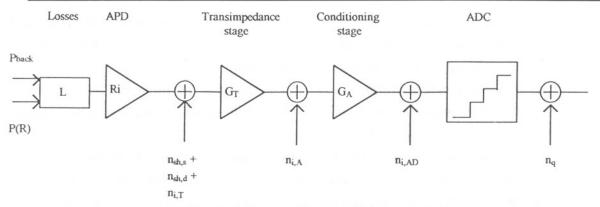


Fig. 14 Lidar receiver and noise sources.

2.5.2. The M-G domain

In this section, the variable G represents the transimpedance or total chain gain. The saturation constraint (point 1) can be mathematically stated as

$$V(R_{\min}) = 2V_{sat} \rightarrow P(R_{\min})LR_{io}MG = 2V_{sat}$$
(43)

where at R_{min} the background power is assumed to be negligible in front of the lidar return, $P(R_{min})$, and $2V_{sat}$ represents the full dynamic range of the analog-to-digital converter (AD).

Assuming an homogeneous atmosphere with visibility margin V_M , substitution of eqs.(7) and (6) into $P(R_{min})$ yields to the *M-G-constraint*

$$MG = A'_{o}; \qquad A'_{o} = f(E, V_{M}, R_{\min})$$
 (44)

Note that different sets of energy, visibility margins and minimum ranges may yield the same system constraint A_o' . From the lidar system's point of view, these three values play the same limiting role. Explicitly, A_o' can be written as follows:

$$A_o' = \frac{A_o}{E}$$
; $A_o = \left(\frac{4V_{sat}h}{A_r L \eta q \lambda}\right) \frac{R_{\min}^2}{\beta} \exp(2\alpha R_{\min})$ (45)

Now, it is wished to relate the saturation constraint to the SNR given in eq.(38). Yet, thermal noise from the transimpedance amplifier, $\sigma_{i,T}^2$, and acquisition card, $\sigma_{i,AD}^2$, must be computed. For the thermal noise system variance at the transimpedance output, we have:

$$\sigma_{th}^2 = \sigma_{i,T}^2 G^2 + \sigma_{i,AD}^2$$
 (46)

Now, this variance can be substituted into thermal noise term of eq.(38). In doing so, one can write

$$\frac{\sigma_{th}^2 B}{R_{io}^2 M^2 G_T^2 L^2} = \frac{d}{M^2 G^2} + \frac{e}{M^2}$$
 (47)

which is expressed in terms of the M-G variables.

Finally, the blending of eqs. (47) and (38) enables to write SNR as function of the multiplication gain, M and the net amplification gain G, only:

$$SNR(M,G) = \frac{P(R)}{\left\{aF(M)[LP(R) + \xi(\lambda)P_{back}] + c'F(M) + \frac{f}{M^2} + \frac{d}{M^2G^2}\right\}^{1/2}}$$
(48)

where:

$$a = \frac{2hcB}{\eta \lambda L^{2}}; \qquad b = \frac{2qBI_{ds}}{R_{io}^{2}L^{2}}; \qquad c' = \frac{2qBI_{db}}{R_{io}^{2}L^{2}}$$

$$d = \frac{\sigma_{i,AD}^{2}B}{R_{io}^{2}L^{2}}; \qquad e = \frac{\sigma_{i,T}^{2}B}{R_{io}^{2}L^{2}}; \qquad f = b + e$$
(49)

Eq.(48) represents the SNR we wanted to optimize at the beginning of this section (point 1). If this equation is linked to the saturation constraint (point 2) of eq.(44), and the following power-law approximation is used for F(M) [145][123]

$$F(M) \approx M^x$$
; $0.17 \le x \le 0.95$ (50)

the optimum gain can be obtained:

$$M = \left(\frac{2f}{ax[LP(R_{\text{max}}, E) + \xi(\lambda)P_{back}] + c'x}\right)^{\frac{1}{2+x}} \rightarrow G = \frac{A'_o}{M}$$
 (51)

For the photodiode considered the x-factor measured was x=0.423 (Tab.2), which is well within the interval given according to [149]. From the same reference, it is also quite close to the x-factor of a silicon APD reach-through structure (x=0.3).

The pair M-G, written in eq. (51) represents the solution of the problem stated before. For any range R, eq. (51) dictates the best photodiode gain, that maximizes the system SNR at a given range R. In the present case, $R=R_{max}$ is the maximum range within the AD-converter dynamic range.

Fig.15 and Fig.16 illustrate the behaviour discussed. Basically, Fig.15 from [20] illustrates the optimum photodiode gain for each optical power. Graphs in Fig.16 show the M-domain according to eq.(51) that provides maximum SNR for the energies and maximum ranges shown. The plots are computed based on Tab.2 at $\lambda = 532$ nm and $V_M = 5km$. From the discussion above, energy and maximum range, R_{max} , together are equivalent to talking of a certain optical power. For this reason, the optimization could also have been done for different optical powers and Fig.15 would have been reencountered.

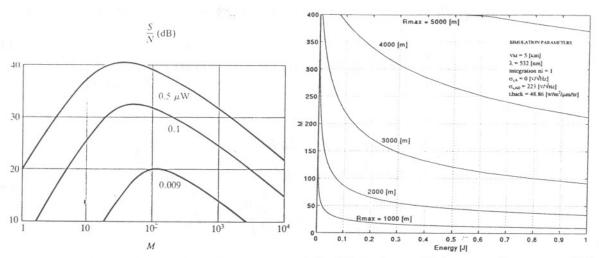


Fig. 15 Sensitivity of APD detector.

Fig. 16 Optimum Gain according to eq. (51).

2.5.3. Present case: the M-G2 domain

Let us consider, now, the complete lidar receiver of Fig.13. The inclusion of the conditioning amplifier following the transimpedance amplifier, must take into account these two points:

a) The receiver equivalent noise given by eq.(46) becomes

$$\sigma_{th}^2 = \sigma_{i,T}^2 G_T^2 + \sigma_{i,A}^2 + \frac{\sigma_{i,AD}^2}{G_A^2}$$
 (52)

b) The inclusion of the conditioning amplifier may convey an additional saturation constraint if the output voltage swing of the transimpedance amplifier is smaller than the input voltage swing of the conditioning amplifier. This is to say, that under certain conditions, the acquisition card may not be saturated but the transimpedance stage can instead. A posteriori, the author advances that this has been the case of the lidar receiver under study. Let $V_{sat} = \pm I$ be the maximum output swing of the transimpedance stage. Then, the amplifier saturation constraint can be written as

$$P(R_{\min})LR_{io}MG_T \le V_{sat,1} \rightarrow MG_T \le A_1$$
 (53)

As in Sect.2.3.2, the goal is to maximize the SNR

$$SNR(M, G_T, G_A) = \frac{P(R)}{\left\{aF(M)\left[LP(R) + \xi(\lambda)P_{back}\right] + c'F(M) + \frac{b_1}{M^2} + \frac{d_2}{M^2G_T^2} + \frac{d_3}{M^2G_T^2G_A^2}\right\}^{1/2}}$$

or, equivalently, to minimize the noise variance. Substitution of (52) into (38) yields the formulation of the minimization problem

$$\min(\sigma^2)\big|_{M,G_{\underline{T}},G_{\underline{A}}} = \left\{ a_1(R)M^x + \frac{b_1}{M^2} + \frac{d_2}{M^2G_T^2} + \frac{d_3}{M^2G_T^2G_A^2} \right\}$$
 (55)

in the feasible domain given by the constraints:

- eqs. (44), (53) or saturation constraints and,

- $M \in (1, M_{max})$; $G_T \in (t_{min}, t_{max})$; $G_A \in (a_{min}, a_{max})$ or gain constraints.

where

$$d_{1} = \frac{\sigma_{i,T}^{2}}{R_{io}^{2}L^{2}}; \qquad d_{2} = \frac{\sigma_{i,A}^{2}B}{R_{io}^{2}L^{2}}; \qquad d_{3} = \frac{\sigma_{i,AD}^{2}B}{R_{io}^{2}L^{2}};$$

$$a_{1} = a[LP(R) + \xi(\lambda)P_{back}] + c'; \qquad b_{1} = b + d_{1}$$
(56)

The constants a, b, c' have already been defined in eq.(49). The variable G of eq.(44) represents net amplification gain due to both transimpedance and conditioning stages, $G = G_T G_A$.

The gain constraints depend on the minimum and maximum gains of the amplification stages. Note that eq.(55) is the counterpart of the denominator of eq.(48).

The tri-dimensional constrained optimization is solved by link-budget software whose code is MATLAB based.

2.6 Default values concerning this section

Tab.2 summarizes default values of the simulations presented.

- NOTES: 1) Link-budget simulations have considered worst case noise variances. They assume maximum gains in the amplifiers and hence simulations offer conservative lidar range estimations.
 - 2) Link-budget simulations shown here assume: $\eta = 54.9 \%$, $R_{io} = 237 \text{ mA/W}$ and $\lambda = 532 \text{nm}$.

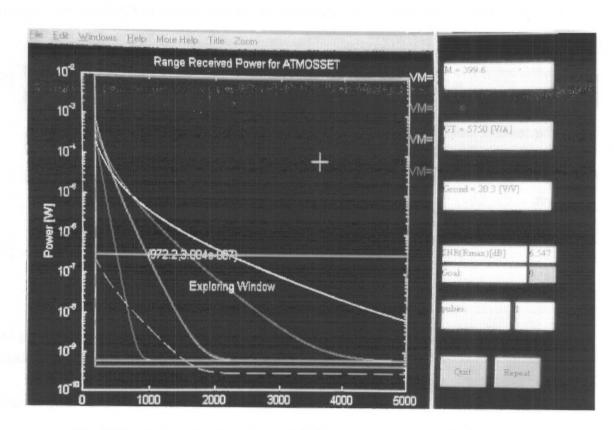


Fig. 17 Exploring window and SNR optimization in link-budget software.

PHOTODETECTOR PARAMETERS APD parameters (measured values unless otherwise indicated) Type: C30954E EG&G Optoelectronics. Silicon, double-diffused reach-through structure. Diameter: ø0.8 mm (specs) Quantum efficiency: $\eta = 54.9 \pm 2.3 \% (\lambda_1 = 532 \text{nm}) \qquad \eta = 30.0 \pm 1.3 \% (\lambda_2 = 1064 \text{nm})$ Intrinsic responsivity (eq.(23)): $R_{io} = 237 \pm 12 \text{ mA/W} (\lambda_1)$ $R_{io} = 258 \pm 13 \text{ mA/W} (\lambda_2)$ Gain performance: a) multip. factor (eq.(22)): $M \in [1 \text{ to } 400] \text{ (for PINs, } M=1).$ b) k-factor (eq.(33)): k = 0.033x = 0.423c) x-factor (eq.(50)): Dark current(eq.(25)): a) surface dark current: $I_{ds} = 13.8 \text{ nA}$ b) bulk dark current: $I_{db} = 6.0 \text{ pA}$ Noise density (eqs.(24),(27)): $\sigma_d \approx 2 \text{ pA Hz}^{-1/2}$, M=400 (specs: $\sigma_d \approx 1 \text{ pA Hz}^{-1/2}$, M=120) Noise Equivalent Power (eq.(29)): $NEP_{532}=21 \text{ fW/Hz}^{1/2} \text{ (M}=400) \quad B \approx 500 \text{ MHz}$ Transimpedance amplifier specs (measured values unless otherwise indicated) Gain: Variable from 750 to 5750 Ω $\sigma_{\rm th}\!=\!5.27~{\rm pA~Hz^{-1/2}}$ (at maximum gain, ${\rm G_T}\,=\,5750\Omega)$ Equivalent input noise: Equivalent noise bandwidth: B=20 MHz

Tab.2 Defaults used link-budget simulations of Sect.2.

3. LIDAR RANGE ESTIMATION

3.1 Absolute minimum and maximum exploring ranges of the system

Eqs.(44) and (53) or saturation constraints enable to mathematically formulate the absolute minimum system range, $R_{min}{}^a$. The superscript a indicates absolute. For each output energy, E, $R_{min}{}^a$ is determined by saturation of either an amplification stage or the acquisition card itself when all the system gains (M, G_T, G_A) are set to minimum. Obviously, which of the two constraints becomes dominant depends on the input and output swings of the components involved in the receiving stages. Yet, let us assume a $\pm 1-V$ input range for the acquisition card, a minimum conditioning gain of less than 3V/V and a $\pm 3-V$ output swing for the transimpedance amplifier. These ranges are pessimistic considering the state-of-the-art in operational amplifiers [135][134][106]. In the example, it turns out that only acquisition card constraint of eq.(44) applies. Note that $R_{min}{}^a$ attains the lowest value when the system gain is minimum. Fig.18 plots absolute minimum system ranges for different output energies and visibility margins based on Tab.3.

On the other hand, the absolute maximum system range, $R_{max}^{\ a}$ is determined by the locus of signal-to-noise ratio equal to some lower bound, SNR. This lower bound is usually SNR=1, even though signal-to-noise ratio at $R_{max}^{\ a}$ can be improved by pulse integration. Since the return signal from $R_{max}^{\ a}$ is very dim, there is no significative signal-induced shot noise (eq.(37)). Under these conditions, SNR is thermal-noise limited (eq.(42)). Then, $R_{max}^{\ a}$ can be computed by setting $SNR(R_{max}^{\ a})=1$ in eq.(54) or equivalently, from the system NEP_s . This concept is similar to the photodiode NEP given in eq.(29). Reconsidering eq.(37), NEP_s can be written as

$$NEP_{s} = \frac{\left[(\sigma_{sh,d}^{2} + \sigma_{i,T}^{2}) G_{T}^{2} G_{A}^{2} + \sigma_{i,A}^{2} G_{A}^{2} + \sigma_{i,AD}^{2} \right]^{1/2}}{R_{io} M G_{T} G_{A}} \qquad \left[\frac{W}{\sqrt{Hz}} \right]$$
 (57)

Note that NEP_s is minimum at maximum system gain. It is important to emphasize that this affirmation does not contradicts Sect.2.5. There, it was suggested that for any $R_{max} < R_{max}^{\ a}$ one can enhance SNR by adjusting the right multiplication gain, M. In the optimization procedure, multiplication gains below the maximum gain suggest that the system is still far from the thermal-noise limited mode. Otherwise, if the optimization were performed at $R_{max}^{\ a}$ range, which is very often of several kilometers, the result would have been that all gains should be as high as possible in order to counteract thermal noise. Quite often, this well-known result from the Friis formula is taken for granted [7].

Similarly to Fig. 18, Fig. 19 plots absolute maximum range versus output energy and visibility margin. Fig. 20 represents the differential range $R_{max}^{\ a}-R_{min}^{\ a}$.

It is important to warn here, that R_{min}^{a} and R_{max}^{a} do not take into account optical limitations, mainly overlap factor (Sect. 1.2). For the time being, this factor is assumed unity over the entire range $(R_{min}^{a}, R_{max}^{a})$. Otherwise, the received signal will be distorted.

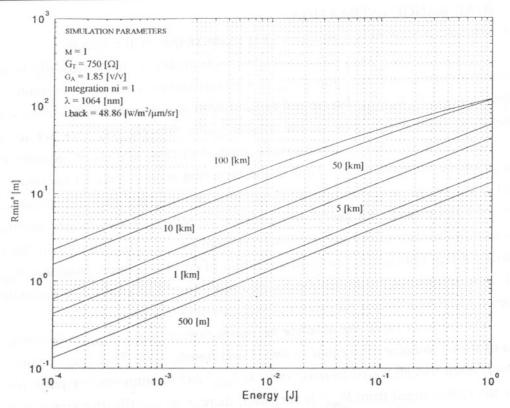


Fig. 18 R_{min} a vs. energy and visibility margin.

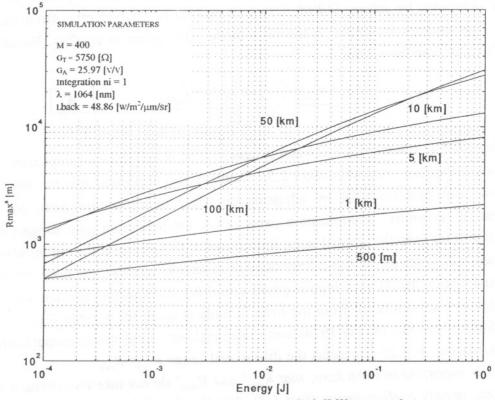


Fig. 19 R_{max}^{a} vs. energy and visibility margin.

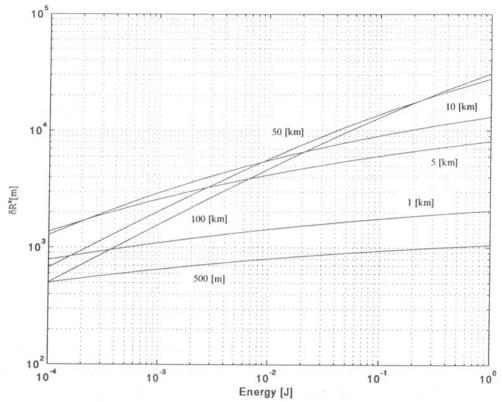


Fig. 20 Differential range $\Delta R^a = R_{max}^a - R_{min}^a$ vs. energy and visibility margin.

3.2 The exploring window

Absolute system ranges are sometimes unpractical limits. In fact, they assess maximum system performance given some knowledge about the visibility margin. The visibility turns out to be an additional uncertainty factor unless transmittance measurements are readily available. In addition, the exploration cannot directly be made from $R_{min}^{\ a}$ to $R_{max}^{\ a}$ because of the limited dynamic range of the acquisition system. One can see the acquisition system as window that explores a determinate segment (from R_{min} to R_{max}) of the absolute system ranges, $R_{min}^{\ a}$ to $R_{max}^{\ a}$. The synchronization system anchors the window to the desired R_{min} . The larger the dynamic range, the larger the segment. Since every bit of and AD-converter equals 6 dB dynamic range, a card with 12 bits will have and input range of 72 dB. This outweighs the specifications of even the best logarithmic amplifiers in the market [115]. Since the logarithmic conversion can ultimately be made in a computer, this option has been discarded in favour of a card with 12 or more bits. Tab.3 lists some specifications of the card chosen.

Fig.17 shows many features of the exploring window in *link-budget* software. Basic inputs to the exploring window procedure are laser energy and a set of visibility margins, the user will choose from. Other system parameters are taken from system default files. Maximum and minimum system detectable powers are indicated by top and bottom lines. These values are absolute limits and correspond to minimum and maximum system gains, respectively.

The exploring window is represented there by a rectangle, whose top left corner the user can anchor at the wished R_{min} and V_M curve, using the mouse. Once the user has chosen these two parameters, R_{max} is computed from the intersection between the exploring window and the power curve for that visibility, V_M . After that, the system gains, M, G_T , G_A are computed according to the M-G2 procedure (Sect.2.5.3) and the equivalent system noise (eq.(37)) is drawn in the screen with a dashed line. Note that this noise, especially at short ranges, may be much higher than the power levels obtained from NEP_s computations because shot noise is usually very large at these ranges.

Once the system gains are computed, they are displayed and they are ready to be set in the lidar equipment. SNR at R_{max} is also shown in the screen. From this value and the minimum SNR wished at R_{max} , SNR_{goal} , the program computes the number of pulses to be integrated, if any. Let n_i the number of pulses and let us assume that the SNR is measured at the system output as a ratio of voltages. Then,

$$10\log(n_i) = SNR_{goal} - SNR(R_{max})$$
 (58)

After that, the system gains, M, G_T , G_A and the number of integrations, n_i , are readily available. They are key parameters of the system. Since, due to the uncertainty in the visibility margin the sought-after gains can change, remote digital control over them would be highly valuable. For example, a GPIB high voltage power supply could serve the purpose to control the APD gain and a programmable lidar receiver should be considered. Of course, the lidar system makes do with analog control over its amplifiers (e.g. multi-turn potentiometers) but doing so, would make the M-G2 optimization cumbersome, if not impossible.

All in all, the tricky parameter in the optimization procedure is the visibility margin. Ideally, it has to be determined from in-situ measurements, e.g. transmitometers or balloon-borne measurements. Otherwise, work with a digitally controlled lidar equipment will provide valuable expertise.

3.3 Gain and synchronism specs

Maximum detectable level complies with the acquisition card constraint of eq.(43). Yet, minimum detectable power may well be buried into the system noise level. If so, thermal noise realizations will have to be integrated in order to retrieve the signal. Moreover, if the integration is wished to succeed, noise clipping must be avoided, otherwise noise statistics will no longer be gaussian. Based on simulations, if minimum detectable power excites $\kappa > 8$ levels of the digitizer, clipping is virtually eliminated. This factor κ is called the *crest-factor*. For the maximum and minimum power, one can write:

$$P_{\text{max}} = \frac{2V_{sat}}{LR_{io}M_{\text{min}}G_{\text{min}}} \qquad P_{\text{min}} = \left(\frac{2Vsat}{2^{bits} - 1}\kappa\right) \frac{1}{LR_{io}M_{\text{max}}G_{\text{max}}}$$
(59)

For the GaGe Compuscope 1012 digitizer (Tab.3), V_{sat} can be programmed within the range 5 V, 1 V, 500 mV, 200 mV and 100 mV. From the beginning, it was agreed that the design should be carried out using operational amplifiers. Considering that typical output voltage ranges for them are between ± 6 , ± 13 V (no load) and between ± 4.5 , ± 8 V (100- Ω load) [134][135], the saturation voltage of the card was chosen to be V_{sat} =1V. This allows conventional system design based on typical 75 or 50 Ω impedances.

Next, let us give some insight on how the receiver gain can be assessed: In Fig.7 (E=500 mJ, λ =532 nm), P_{min} is less than 1~mW for $R_{min}^{a} \approx 200~m$. This minimum range may be considered a sensible choice since lower ranges may well fall into the range interval where the overlap factor has not settled yet (case 3 in Sect.1.2). Anyhow, let us consider that P_{min} may be as high as 5~mW under a more conservative criterion.

As for R_{max}^{a} , the design specification is $R_{max}^{a} \approx 5 \ km$ under average seeing conditions. This goal has been set because R_{max}^{a} is well above the boundary layer and covers most of the meteorological phenomena of interest.

Since the higher range is the most difficult range to assess *a priori*, during the link-budget stage of the project a conservative visibility margin was considered. Even though V_M lies between 15 and 23.5 km (Fig.6) for average seeing conditions, $R_{max}^{\ a}$ condition was computed with a V_M as low as 5-10 km (light-moderate haze), given an output energy of 1 J (λ =1064 nm and Fig.8). Under these assumptions and the plots of Fig.7, P_{min} is about 1-5 nW for E = 500 mJ and about 2-10 nW for E = 1J, since the APD has similar responsivities at both operating wavelengths. Looking to these figures, $P_{min} = 5$ nW, seems a reasonable choice. Summing up, the system is specified to cope with approximate power levels in the interval:

$$P \in (5 \text{ mW}, 5 \text{ nW}).$$

Assumming L=0.3, $R_{io}=0.3$ (specs), $M\epsilon(1,120)$ (specs), $V_{sat}=1V$, $\kappa=8$, eq.(59) yields the following MG and G gains, where $G=G_TG_A$:

$$MG \le 4400 \ \Omega; \ MG \ge 8.7x10^6 \ \Omega$$

 $G_{min} \le 4400 \ \Omega; \ G_{max} \ge 72x10^3 \ \Omega$

These results are also shown in Tab.3. Note that the final performance of the system will ultimately depend on the measured multiplication gain, M. In fact, Tab.2 and Tab.3 evidence a mismatch between the maximum multiplication gain reported by the manufacturer and the measured one.

To have an estimate of the system NEP, NEP_s , G_{max} can be split as $G_T = 4000~\Omega$ and $G_A = 18~V/V$. If the values specified (Tab.2,Tab.3) are considered M = 120, $\sigma_{i,T} = 5.27$ $pA~Hz^{-1/2}$, $\sigma_{i,A} = 3.41~nV~Hz^{-1/2}$, $\sigma_{i,AD} = 90~nV~Hz^{-1/2}$, the system NEP becomes, $NEP_s = 220~fW~Hz^{-1/2}$, which under a noise equivalent bandwidth of 9.2 MHz, leads to a noise power

of 0.6 nW (SNR= 9.2 dB). Note that the same R_{max}^{a} could have been derived from a family of plots similar to Fig.19 using the criterion $SNR(R_{max}) = 9.2 dB$. If the measured multiplication gain, M=400, is considered (Tab.2, Tab.3) $NEP_s = 70 fW Hz^{-1/2}$.

All in all, $R_{min}^{\ \ s}$ and $R_{max}^{\ \ s}$ are equivalent to time-delays of 0.66 μs and 13.3 μs , respectively.

RECEIVER AND SYNCHRONISM PARAMETERS

Acquisition card: GaGe CompuScope 1012, 20 Msps, 12 bits

Dynamic input range: 72 dB (6 dB/bit)

Input scales: $\pm 5V$, $\pm 1V$ (range chosen), ± 500 mV, ± 200 mV, ± 100 mV

Noise: $\sigma_{i,AD} = 223 \text{ nV Hz}^{-1/2} \text{ (measured)}, 90 \text{ nV Hz}^{-1/2} \text{ (specs}^*)$

Receiver: (link-budget computations assume visibility margin, $V_{M} \approx 5 \text{ km}$)

Estimated system absolute ranges and typical power levels (Fig.7, Fig.8):

 R_{min}^{a} < 200 m (P \approx 5 mW) R_{max}^{a} \geq 5 km (P \approx 5 nW)

Assumming L=0.3, $R_{io}(specs^*)=0.3$ A/W, $M(specs^*)\epsilon(1,120)$, $V_{sat}=1V$, $\kappa=8$ (eq. (59))

Chain gain, M·G (G= G_TG_A): MG $\leq 4400 \Omega$; MG $\geq 8.7 \cdot 10^6 \Omega$

if M ϵ (1,120) then $G_{min} \leq 4400 \Omega$; $G_{max} \geq 72 \cdot 10^3 \Omega$

Further specs: Variable gain between G_{min} , G_{max} and offset (-1 V level shift).

Noise: a) transimpedance stage $\sigma_{i,T} = 5.3 \text{ pA} \cdot \text{Hz}^{-1/2}$ (measured)

b) conditioning stage $\sigma_{i,A} = 3.4 \text{ nV Hz}^{-1/2}$ (measured)

 $NEP_s \approx 220 \text{ fW} \cdot Hz^{-1/2} \text{ (eq.(57))}$ at $(MG)_{max} (M=120, G_T=4000\Omega, G_A=18 \text{ V/V})$

 $NEP_s \approx 70 \text{ fW} \cdot Hz^{-1/2}$ (measured) (as above but using measured M = 400)

Synchronization unit:

 $R_{min}^{s} = 100 \text{ m} (0.66 \mu s)$ $R_{max}^{s} = 2 \text{ km} (13.3 \mu s)$

^{*} The note (specs) indicates that the value has been taken from the device data sheet. Measurement of the parameter at a later time revealed a different figure. The new figure is indicated as (measured) into brackets. Most figures have been advanced from subsequent chapters. The plots presented in this chapter include updated values and show actual performance.

4. A glance to link-budget software

Link-budget software, from which all the plots presented in this chapter have been processed, offers many possibilities to study lidar systems. It basically concentrates on the optical and electric stages of the lidar receiver. Link-budget along with link-atmos (radiance and atmospheric studies) and link-detect (inversion algorithms) build the link-lidar main package developed during this PhD thesis. About link-budget possibilities:

- 1) Defaults. Lidar system parameters and photodiode libraries can be readily up-to-dated using pop-up menus. For examples, visibility pop-up menus include tabulated values of (V_M, α, β) vs. wavelength.
- 2) Sweep range. Absolute system ranges, R_{min}^{a} , R_{max}^{a} are assessed. Results can be parameterized for any lidar parameter and hence effects on the overall system performance can easily be pinpointed.
- 3) Lidar and the atmosphere. Exploring window (Sect. 3.2) and signal-to-noise studies are included.
- 4) Overlap factor. (Sect.1.2).
- 5) Stochastic simulator. Electrical signals at different points of the lidar receiver of Fig.13 are simulated. Random noise generators simulate APD and amplifier noises and hence SNR can be estimated.

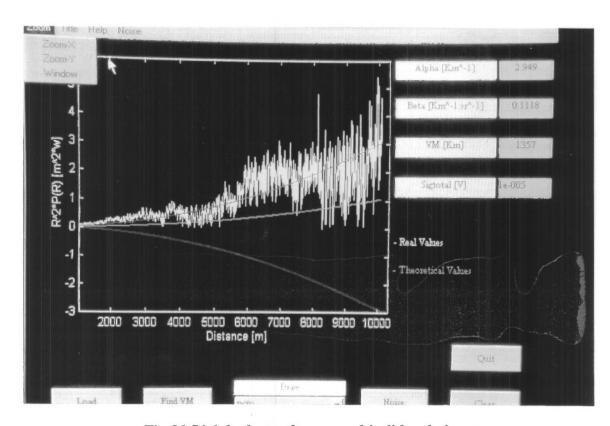


Fig. 21 Link-budget software used in lidar design.